



# Reliability, Precision and the Neuronal Code

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## Introduction

Cortical neurons may use a rate code or a spike time code (for review see Shadlen & Newsome (1998)). A spike-time code is only possible when neural discharge is reliable. The discharge of neurons driven by a constant drive is unreliable, whereas it is reliable when driven by a random fluctuating drive (Mainen & Sejnowski (1995); Cecchi et al (2000)). A neuron driven by a sinusoidal current has a reliability resonance when it produces one spike per drive cycle (Nowak et al (1997); Hunter et al (1998); Fellous et al (2001)). Here we study the behavior of the reliability in terms of attractor dynamics and bifurcations.

## Methods

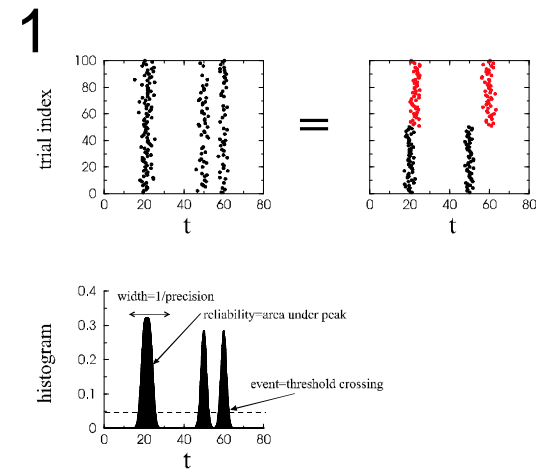
The dynamics of an integrate-and-fire neuron is

$$\dot{V} = -V + A f(t) + \xi$$

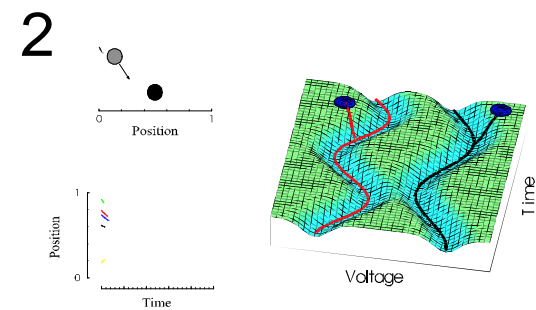
$V$  is the membrane potential,  $f(t)$  is a fluctuating drive,  $A$  is its amplitude,  $I$  is a constant depolarizing current,  $\xi$  is a white noise current with variance  $D$ . When  $V$  reaches threshold,  $V=1$ , a spike is emitted and the voltage is reset to  $V=0$ . Dimensionless units were used, 1 voltage unit corresponds to 20 mV and 1 time unit corresponds to 10-40 ms. Experimental recordings were performed as in Fellous et al (2001).

## References

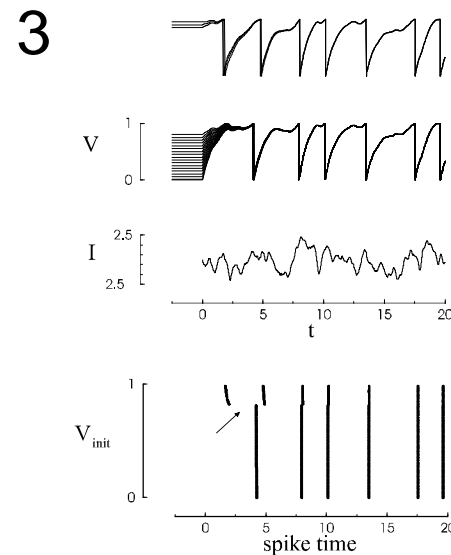
Cecchi, G., et al (2000). Proc. Natl. Acad. Sci., 97:5557-5561.  
Coomes, S. and Bressloff, P. (1999). Phys. Rev. E, 60:2086-2096.  
Fellous, J.-M., et al (2001) J. Neurophys., 85:1782-1787  
Hunter, J., et al (1998). J. Neurophysiol., 80:1427-1438.  
Mainen, Z. and Sejnowski, T. (1995). Science, 268:1503-1506.  
Nowak, L., et al (1997). Cereb. Cortex, 7:487-501.  
Shadlen, M. and Newsome, W. (1998). J. Neurosci., 18:3870-3896.



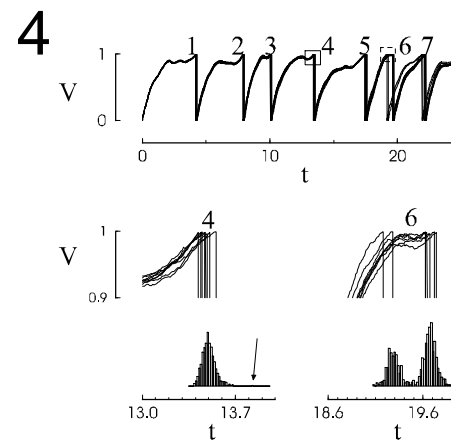
Deterministic structure of spike trains is not detected in the spike time histogram (STH) or using reliability measures based on the STH.



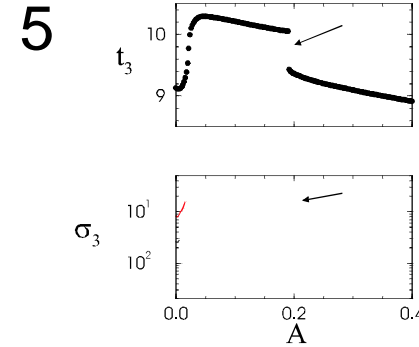
An attractor can be conceptualized as a river valley. From different initial conditions the ball rolls into the valley and follows the river flow.



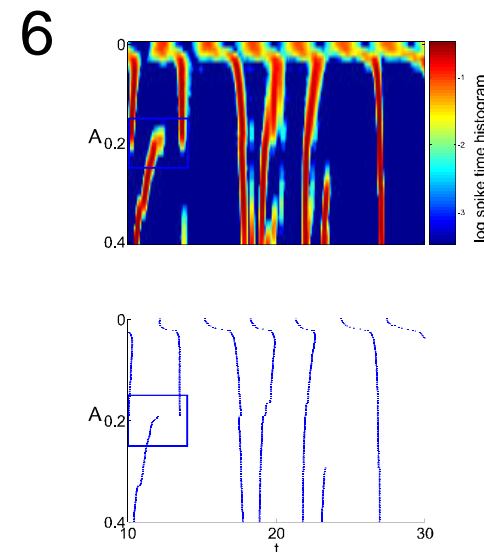
Voltage of an integrate-and-fire model neuron converges from different initial conditions to a single attractor. Reproducible spike trains are obtained.



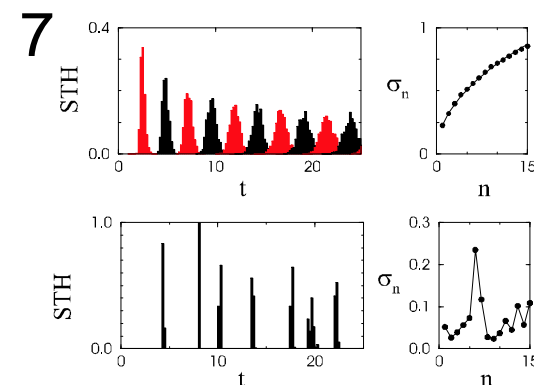
Intrinsic noise induces deviations from the attractor: (1) Distinct spike trains are obtained. (2) Reliability is reduced. (3) Spike-time jitter is not proportional to noise standard deviation.



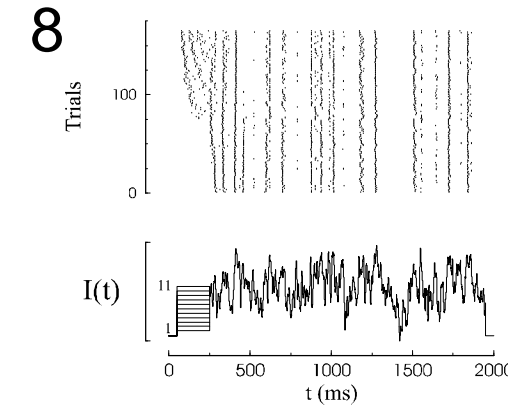
During a bifurcation spike time  $t_3$  changes discontinuously when a parameter is varied. Close to a bifurcation point reliability is reduced and jitter  $\sigma_3$  is increased.



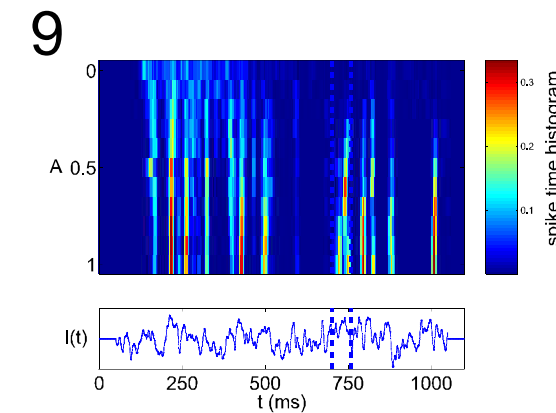
Bifurcation structure explains variation of the reliability with drive amplitude  $A$ .



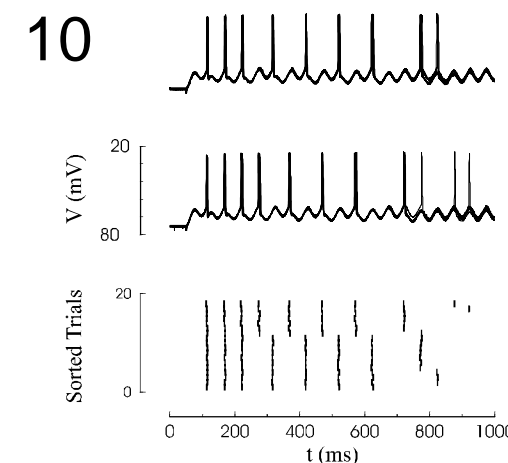
Attractor stability governs asymptotic precision.



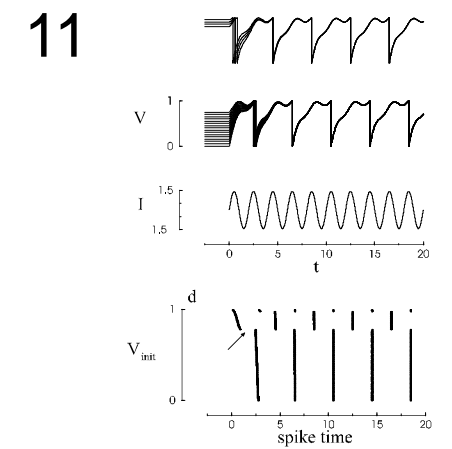
(Experiment) Spike trains recorded from cortical neurons in vitro converge from different initial conditions to similar spike trains.



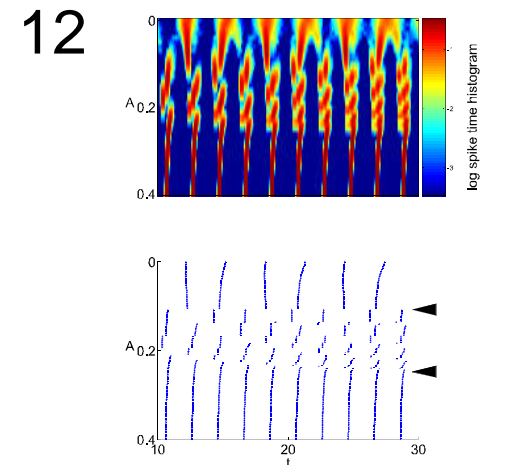
(Experiment) Bifurcations are observed in recordings from cortical neurons when the drive amplitude is varied.



(Experiment) During 1:2 mode-locking there are two attractors.



Depending on initial condition one of two attractors are reached during 1:2 mode-locking.



Density of bifurcation points is non uniform for a periodically driven model neuron. A reliability resonance peak for 1:1 entrainment is obtained.

## Summary

- Neuronal dynamics can be characterized in terms of attractors and bifurcations.
- Reliability is inversely proportional to the number of distinct output signals produced across trials.
- Reliability is the noise stability of attractors. A neuron confined to one attractor produces a unique output spike train.
- Reliability is reduced close to a bifurcation point.
- Periodic, random fluctuating and constant drives yield different bifurcation structures.